

**11.19. Model:** Use the definition  $F_s = -dU/ds$ .

**Visualize:** Please refer to Figure EX11.19.

**Solve:**  $F_x$  is the negative of the slope of the potential energy graph at position  $x$ .

$$F_x = -\left(\frac{dU}{dx}\right)$$

Between  $x = 0$  m and  $x = 3$  m, the slope is

$$\text{slope} = (U_f - U_i)/(x_f - x_i) = (60 \text{ J} - 0 \text{ J})/(3 \text{ m} - 0 \text{ m}) = 20 \text{ N}$$

Thus,  $F_x = -20$  N at  $x = 1$  m. Between  $x = 3$  m and  $x = 5$  m, the slope is

$$\text{slope} = (U_f - U_i)/(x_f - x_i) = (0 \text{ J} - 60 \text{ J})/(5 \text{ m} - 3 \text{ m}) = -30 \text{ N}$$

Thus,  $F_x = 30$  N at  $x = 4$  m.